

To be preserved.

Received 6 Novemb 1876

[24.2a]

J. M. Mills

Sec R S E

The Secretary, R. S. E.

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(archive)

Opened by Leon Jones

15/10/87

P. S. Fair.

[24.26]

Opened by Jean Jones 15/10/1987  
(archivist)

MM

Noted by Professor Yait -  
put into the hands of the  
Secretary of the Royal Society  
Monday 16<sup>th</sup> October 1876.

Private.

24.3a

From Prof. J. R. Fraser.

(See Minutes of Council, 6/12/94)

Recd from Prof. Cairns  
on Monday 16 Oct. 1876

J. M. Muller

The Theory of Knots

By Prof. Cairns.

Royal Society

Oct. 16<sup>th</sup> 1876.

Substance for a clear coil.

A B C -- B -- A -- C --  
± ± ± ± ± ± ±

5 laws for simplification.

Irreducible to

+++ ---

Openable.

If the simplest is

+ - + - + - + - irreducible.

11/11/76.

Let  $\theta, \phi, \dots$  be gen<sup>l</sup> coord<sup>s</sup>.  $T$  a hom<sup>o</sup> quad<sup>c</sup> fct<sup>n</sup> of  $\dot{\theta}, \dot{\phi}, \dots$  & not involving  $t$  explicitly.

$$\text{Then } 2T = \sum \dot{\theta} \left( \frac{dT}{d\dot{\theta}} \right)$$

Hence

$$\sum \dot{\theta} \left( \frac{dT}{d\dot{\theta}} \right) = 2T = T + H - V.$$

Diffs

$$\sum \left\{ \ddot{\theta} \left( \frac{dT}{d\dot{\theta}} \right) + \dot{\theta} \frac{d}{dt} \left( \frac{dT}{d\dot{\theta}} \right) \right\} = \sum \left\{ \frac{dT}{d\dot{\theta}} \ddot{\theta} + \left( \frac{dT}{d\dot{\theta}} \right) \ddot{\theta} - \left( \frac{dV}{d\dot{\theta}} \right) \dot{\theta} \right\}$$

$$\text{or } \frac{d}{dt} \left( \frac{dT}{d\dot{\theta}} \right) = \frac{dT}{d\dot{\theta}} - \frac{dV}{d\dot{\theta}}$$

Again

$$\begin{aligned} \delta A &= \delta \int 2T dt = \delta \int (T + H - V) dt \\ &= \int \left( \delta H + \sum \left\{ \delta \theta \left( \frac{dT}{d\dot{\theta}} \right) - \delta \theta \left( \frac{dV}{d\dot{\theta}} \right) + \delta \dot{\theta} \left( \frac{dT}{d\dot{\theta}} \right) \right\} \right) dt \\ &= \sum \delta \theta \left( \frac{dT}{d\dot{\theta}} \right) + t \delta H \\ &\quad - \sum \int \delta \theta dt \left( \frac{d}{dt} \left( \frac{dT}{d\dot{\theta}} \right) - \left( \frac{dT}{d\dot{\theta}} \right) + \left( \frac{dV}{d\dot{\theta}} \right) \right) \end{aligned}$$

of which the unintegrated part vanishes by the former part.

P.S.V.