

Errata for Exact Sequences in the Algebraic Theory of
Surgery
by Andrew Ranicki
Mathematical Notes 26, Princeton (1981)

This list contains corrections of misprints/errors in the book. Please let me
know of any further misprints/errors by e-mail to a.ranicki@ed.ac.uk

A.A.R. 7.4.2006

- p. 4, l. -11 $H^{r+1}(f)$
- p. 5, l. -5 $T_\epsilon : \text{Hom}_A(C^p, C_q) \rightarrow \text{Hom}_A(C^q, C_p) ; f \mapsto (-1)^{pq}\epsilon f^*$
- p. 5, l. 3 $C_p^t \otimes_A D_q$
- p. 5, l. -2, -3 $\begin{cases} \epsilon\text{-symmetric} \\ \epsilon\text{-quadratic} \\ \epsilon\text{-hyperquadratic} \end{cases}$
- p. 14, l. 11 $\begin{cases} \epsilon\text{-symmetric} \\ \epsilon\text{-quadratic} \\ \epsilon\text{-hyperquadratic} \end{cases}$
- p. 31, l. 10 $\dot{\psi}_F(x, y, z) = (\Sigma_Y^p \dot{\Delta}_Y(y) - F^% \Sigma_X^p \dot{\Delta}_X(x), F^% h_X^p(x) - h_Y^p(y) - \dot{\Delta}_{\Sigma^p Y}(z))$
- p. 31, l. 13 replace Ω by Σ
- p. 46, l. 7 $\begin{cases} (\delta\phi/\phi)_s = \begin{pmatrix} \delta\phi_s & \cdot \\ \cdot & \cdot \end{pmatrix} \\ (\delta\psi/\psi)_s = \begin{pmatrix} \delta\psi_s & \cdot \\ \cdot & \cdot \end{pmatrix} \end{cases}$
- p. 47, l. -1 $\partial C_r = C_{r+1} \oplus C^{n-r}$
- p. 54, l. -8 Proposition 1.2.3 i), ii)
- p. 61, l. 8 $f^* \phi' f = \phi \in Q^\epsilon(M)$
- p. 76, l. -5 Highly-connected Poincaré complexes
- p. 78, l. 10 $\delta\phi_s'' = \begin{pmatrix} \delta\phi_s & 0 & 0 \\ (-)^{n-r} \phi'_s f_{C'}^* & (-)^{n-r+s} T_\epsilon \phi'_{s-1} & 0 \\ 0 & (-)^s f'_{C'} \phi'_s & \delta\phi'_s \end{pmatrix}$
- p. 78, l. -2 $D'^{n-r-s+1}$
- p. 99, l. 5 $\text{Hom}_B(D^*, D)_{n-s}$

p. 116, l. 7 $C \xrightarrow{f} D$

$$\text{p. 119, l. 6-9 } \delta\nu_s'' = \begin{pmatrix} \delta\nu_s & 0 & 0 \\ (-)^{n-r+1}\phi'_s h'^* & (-)^{n-r+s+2}T_\epsilon\delta\phi'_{s-1} & 0 \\ 0 & (-)^s\tilde{h}'\phi'_s & \delta\nu'_s \end{pmatrix}$$

$$\text{p. 119, l. 12-15 } \delta\chi_s'' = \begin{pmatrix} \delta\chi_s & 0 & 0 \\ (-)^{n-r+1}\psi'_s h'^* & (-)^{n-r+s+1}T_\epsilon\delta\psi'_{s+1} & 0 \\ 0 & (-)^s\tilde{h}'\psi'_s & \delta\chi'_s \end{pmatrix}$$

p. 174, l. 10 $\text{im}(\widehat{H}^0(\mathbb{Z}_2; \widehat{S}^{-1}\widehat{A}, \epsilon) \rightarrow \widehat{H}^1(\mathbb{Z}_2; A, \epsilon)) = 0$

p. 190, l. 6 $0 \leq r \leq n+1$

p. 190, l. 9 (P, Q, f, g, h, i, j, k)

p. 191, l. 5 $Q_0 = D_1 \oplus D_3 \oplus D_5 \oplus \dots$

p. 192, l. -1 $\phi \mapsto (\epsilon\widehat{\phi}; x \mapsto (y \mapsto (-)^{pq}\epsilon\overline{\phi(y)(x)}))$

p. 230, l. 11 complexes

p. 252, l. -5 $(F, (\begin{pmatrix} -\gamma \\ \mu \end{pmatrix}, -\theta)G) \oplus (F, (\begin{pmatrix} \gamma \\ \mu \end{pmatrix}, \theta')G)$

p. 255, l. 11 with

p. 257, l. -2 $\theta_{-1} : D^0 \rightarrow D_1$

p. 258, l. 2 $\theta_0 - \epsilon\theta_0^* = 0, \tilde{d}\theta_0 - \tilde{\theta}_{-1} + \epsilon\theta_{-1}^* = 0, \theta_0\tilde{d}^* + \theta_{-1} - \epsilon\tilde{\theta}_{-1}^* = 0$

p. 258, l. -4 on the chain level $f_{\%}(\psi'_0) = \theta_{-1}, f_{\%}(\tilde{\psi}'_0) = \tilde{\theta}_{-1}, f_{\%}(\psi'_1) = \tilde{d}\chi\tilde{d}^* - \tilde{\theta}_{-1}\tilde{d}^*$

p. 259, l. 4 with $\delta\psi' = \{\delta\psi'_0 = -\epsilon\chi^*, \delta\psi'_1 = -\chi\tilde{d}^*, \tilde{\delta}\psi'_1 = \tilde{\theta}_{-1}, \delta\psi'_2 = 0\}$

p. 372, l. 5 $\dots \rightarrow \dots \rightarrow \dots \rightarrow$

p. 375, l. 3 $L_n(A, \epsilon)$

p. 420, l. 3 $n \geq -2$

$$\text{p. 431, l. 13 } \left(\sum_{j=0}^{\infty} a_j x^j\right) \left(\sum_{k=0}^{\infty} b_k x^k\right) = \sum_{j=0}^{\infty} \sum_{k=0}^{\infty} a_j \alpha^{-j} (b_k) x^{j+k}$$

p. 445, l. 6 $(C, \nu, \delta\phi, \phi) \mapsto (C_\alpha[x, x^{-1}], [\nu, \delta\phi, \phi]) \oplus (C_\alpha[x, x^{-1}], -\phi)$

p. 445, l. 8 $(C, \nu, \delta\psi, \psi) \mapsto (C_\alpha[x, x^{-1}], [\nu, \delta\psi, \psi]) \oplus (C_\alpha[x, x^{-1}], -\psi)$

p. 457, l. -5 nilcomplexes

p. 477, l. 3 $\rightarrow \dots \rightarrow \dots$

- p. 490, l. -1 $\partial = \partial_f \delta = \widehat{\delta} \gamma_{g'}$
- p. 514, l. -6 $(\theta + \mu^* \psi_B \mu + \chi_B + \epsilon \chi_B^*, \theta' + \mu'^* \psi_{B'} \mu' + \chi_{B'} + \epsilon \chi_{B'}^*)$
- p. 514, l. -2 $\beta^*(1 \otimes_{B'} \theta') \beta - 1 \otimes_B \theta - (1 \otimes_B \mu^*) \psi (1 \otimes_B \mu)$
 $= \beta^*(1 \otimes (\chi_{B'} + \epsilon \chi_{B'}^*)) \beta - 1 \otimes (\chi_B + \epsilon \chi_B^*) \in \text{Hom}_{A'}(A' \otimes_B G, A' \otimes_B G^*)$
- p. 519, l. 4 $(\psi - (\psi + \epsilon \psi^*) \chi (\psi + \epsilon \psi^*), 0)(B^q, \psi' + \epsilon \psi'^*, B'^q)$
- p. 534, l. 1 $L_2(\mathbb{Z}) \oplus L_2(\mathbb{Z}) \rightarrow L_2(\mathbb{Z}_2) \rightarrow L_1(\mathbb{Z}[\mathbb{Z}_2]) \rightarrow L_1(\mathbb{Z}) \oplus L_1(\mathbb{Z})$
- p. 557, l. -3 of
- p. 584, l. 2 $[X, G/TOP] = \mathcal{T}^{TOP}(X) = \mathcal{T}^{TOP}(X, Y, \tilde{\xi}) = H_n(X; \mathbb{L}_0)$
- p. 604, l. -9 $T(\nu_M)$
- p. 606, l. 3 $C(f; \mathbb{Z}_2)$
- p. 622, l. 5 $Q_{n-1}(C') \rightarrow Q^{n-1}(C') \oplus Q_n(SC') \rightarrow Q^n(SC')$
- p. 644, l. 9 is
- p. 663, l. -2 $Wh_*(\pi_1(X)) \rightarrow \widetilde{\text{Nil}}_*(\Phi)$
- p. 669, l. -10 ∂x
- p. 672, l. 8 $1 \otimes_A \psi$
- p. 672, l. -9 $\rightarrow D_k$
- p. 672, l. -8 $\widetilde{B}_k \otimes_A$
- p. 673, l. -10 $D_+ \oplus D_-$
- p. 674, l. -1 $a =$
- p. 677, l. -11 injection, not surjection
- p. 695, l. 10 $p\psi$ not $p^! \xi$
- p. 704, l. -4 The chain map $j : p^! C \rightarrow E$ is ill-defined. It should be replaced by the $\mathbb{Z}[\pi^!]$ -module chain map $j' : p^! C \rightarrow E' = C(f)$ defined by
- $$j' : p^! C_r = p^! D_r \oplus p^! p_! p^! D_{r-1} \oplus p^! p_! E_r \rightarrow E'_r = p^! D_{r-1} \oplus E_r ;$$
- $$(x, a \otimes y, b \otimes z) \mapsto ([a]y, [b]z) \quad (a, b \in \mathbb{Z}[\pi], x \in D_r, y \in D_{r-1}, z \in E_r)$$
- The paper *The L-theory of twisted quadratic extensions* (Canadian J. Math. XXXIX, 345–364 (1987)) contains a generalization of Proposition 7.6.4.
- p. 737, l. -13 $\oplus \widetilde{LNil}_n(A, \alpha^{-1}, \epsilon)$
- p. 738, l. -8 $\widehat{L}^n(p^!)$

p. 739, l. 9 $\pi \times_{\alpha} D_{\infty}$

p. 740, l. 6 $(Q_1; \partial_+ Q_1, \partial_- Q_1) = (M \times \overline{P_1^k - D^k}; \partial M \times \overline{P_1^k - D^k}, M \times S^{k-1})$

p. 740, l. 8 $(Q^{n-2}, \partial Q^{n-3}) = (Q_1 \cup_{M \times S^{k-1}} Q_2, \partial_+ Q_1 \cup_{\partial M \times S^{k-1}} \partial_+ Q_2)$

p. 742, l. -5, -10 $L_{n-2}(\mathbb{Z}[\pi \times_{\alpha} D_{\infty}^{-\epsilon}])$

p. 767, l. 15 obtain

p. 789, l. -9 if $r = 1$ let $g' = \begin{pmatrix} 1 \\ -1 \end{pmatrix} : \mathbb{Z}[\pi'] \rightarrow C(\overline{S^0}) = \mathbb{Z}[\pi'] \oplus \mathbb{Z}[\pi']$

p. 797, l. -9 $(H_{(-)^i}(M'); M', \text{im}(\begin{pmatrix} 1-t \\ \alpha' \psi' + (-)^i t \psi'^* \end{pmatrix} : \alpha' M' \rightarrow M' \oplus M'^{*, w'^{\epsilon}}))$

p. 798, l. -6 $\alpha SC(\widetilde{X})_r = \alpha C_{r-1}$

p. 807, l. 1 $C(g^!)$

p. 811, l. 16 $\nu_{K \subset U} : K \rightarrow BG(2)$

p. 813, l. 4 The asserted “mild generalization of the splitting theorem of Shaneson [1]” is wrong. If $\omega : \pi \rightarrow \text{Aut}(\mathbb{Z}) = \mathbb{Z}_2$ is a non-trivial group morphism the semi-direct product $\pi' = \pi \rtimes_{\omega} \mathbb{Z}$ can also be expressed as a free product with amalgamation $\pi' = \pi *_{\rho} \pi$ of two copies of π along the index 2 subgroup $\rho = \ker(\omega) \subset \pi$ (cf. the two expressions for the infinite dihedral group D_{∞} on p. 739, which is the special case $\pi = \mathbb{Z}_2, \rho = \{1\}$). Cappell’s splitting theorem gives

$$L_n(\mathbb{Z}[\pi'^{w'}]) = L_n(\mathbb{Z}[\pi^w]) \oplus L_n^X(\mathbb{Z}[\rho^v] \rightarrow \mathbb{Z}[\pi^w]) \oplus \text{Unil}_n(\Phi) \quad (n \in \mathbb{Z})$$

with

$$\begin{aligned} w' : \pi' &\longrightarrow \pi \xrightarrow{w} \mathbb{Z}_2, \\ v : \rho &\longrightarrow \pi \xrightarrow{w} \mathbb{Z}_2 \end{aligned}$$

for any map $w : \pi \rightarrow \mathbb{Z}_2, X = \ker(Wh(\rho) \rightarrow Wh(\pi))$ and

$$\begin{array}{ccc} \mathbb{Z}[\rho^v] & \longrightarrow & \mathbb{Z}[\pi^w] \\ \downarrow & \Phi & \downarrow \\ \mathbb{Z}[\pi^w] & \longrightarrow & \mathbb{Z}[\pi'^{w'}] \end{array}$$

The discussion on p. 812–814 should therefore be restricted to the case $\omega = +1$ only.

p. 817, l. 7 $\widehat{\psi}_F : \dot{H}_{n+1}(X/\pi) \rightarrow Q_n^{[0,0]}(C(f)) = \widehat{Q}_n(C(f)) \quad (n \geq 0)$

p. 818, l. -12 $\widetilde{M} \times D^1 \subset \widetilde{W}$

p. 820, l. 2 indeterminate

$$\text{p. 820, l. } -2 \quad \tilde{X} = \bigcup_{j=-\infty}^{\infty} z^j N$$

p. 823, l. 14 delete a

p. 828, l. 1 Seifert [2]